International J. of Math. Sci. & Engg. Appls. (IJMSEA) Vol. 2 No. IV (2008), pp. 199 – 207

DIFFERENTIAL SUBORDINATION CONCERNING UNIFORMLY CONVEX AND UNIFORMLY CLOSE TO CONVEX FUNCTIONS

T. RAM REDDY, P. THIRUPTHI REDDY AND R. B. SHARMA

Abstract

Let $UCV_{\alpha}(h)$ denote the class of all functions $f \in A$ with $\frac{z(k_{\alpha} * f)(z)}{(k_{\alpha} * f)(z)} f h(z)$ where

 $k_{\alpha} = \frac{z}{(1-z)^{\alpha}} \quad (\alpha \text{ is a real number}) \text{ and } h(z) \text{ is a convex function with } h(0) = 1 \text{ and Re}$ $h(z) > 0. \text{ Let } F(z) = \frac{c+1}{z^{c}} \int_{0}^{z} t^{c-1} f(t) dt. \text{ It is proved that } F \in UCV_{\alpha}(h) \text{ whenever } f \in UCV_{\alpha}(h) \text{ and also that } UCV_{\alpha+1}(h) \subset UCV_{\alpha}(h) \text{ for } \alpha \ge 1. \text{ Further more we proved that}$

 $UCC_{\alpha+l}(h) \subset UC C_{\alpha}(h)$ for $\alpha \geq l$

AMS Subject Classification : Primary 30C 45

Key Words : Uniformly Convex, Uniformly Starlike, Uniformly Close to Convex, Subordination and Convolution.